EVALUATION OF MULTIREGIONAL FUZZY CASCADE CONTROL FOR pH NEUTRALIZATION PROCESS

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ABSTRACT
In pH reactors, determination and control of pH is a common problem concerning chemical-based industrial processes due to the non-linearity observed in the titration curve. We introduced a modified multiregional fuzzy-based control system to overcome the complexity of precise control of pH. In order to compensate for the experimental inaccuracies in measurements of pH in-situ values; an observer for pH is implemented using adaptive neuro-fuzzy inference system (ANFIS). The pH control approach and ANFIS-based observer are integrated in a nonlinear cascade structure to ensure the dynamic modifications and stability enhancement. The cascade structure is designed using a multiregional Fuzzy PI controller in the master loop and a Wiener model-based fuzzy proportional controller as a slave one. The multiregional fuzzy cascade control (MFCC) structure is developed to implicate the three main regions of the titration curve.

Keywords: Titration process, Cascade structure, multiregional fuzzy, ANFIS, pH observer.

1. INTRODUCTION
pH control had always drawn attention of chemical engineers because of its significance in various fields as medicine, where the effect of pH on the enzymes and blood is intensely investigated, and the industry which is concerned with manufacturing of textile dyes, and bleach products. Furthermore, several studies had enriched this research area as environmentalists concerns regarding treating waste water and the acidic rain, and recently the enormous interest of the nuclear scientists to gain a safe monitoring of the pH in the nuclear reactors and resulted materials [1]. In such systems, a fundamental concern is the vast variation of pH encountered with titration process; this implies that a small change in the composition specifications in the process could lead to great divergence in pH values which endanger the stability of the system. This arouses curiosity of researchers and engineers who investigated the development of empirical models and proposed various control techniques to be applied with industrial pH processes [2].

Recent studies on the application of Wiener model-based controller considered a measurement delay and proposed an adaptive control system for pH control using neural networks [3-5]. Some researchers introduced a cascade structure to maintain pH at 7 when the titration curve undergoes large variations. The cascade system consists of an inner loop which includes a typical Wiener model with a proportional controller, while the outer loop is a conventional feedback system with a Proportional and Integral (PI) controller. This model had overcome the large oscillations complication resulted from the switching over titration curve from weak to strong acid and vice versa, nevertheless it has some drawbacks with large variations of pH.

Therefore, this paper proposes a multiregional fuzzy-based cascade control system; this approach is accomplished by sectioning the titration curve into three main regions in order to encounter the large variations of pH by ensuring stability improvements. Evaluation of pH as a controlled variable is achieved using an adaptive neuro-fuzzy based pH observer which is validated within the master feedback loop of the proposed control structure as seen in Fig.1. The models are designed and verified numerically with MATLAB/SIMULINK to obtain the optimum design for the neutralization process under study.
Where; $\text{pH}^*$ is the reference value of pH, $\text{DV}$ is the disturbance variable affecting the control signal, $\text{MV}$ is the manipulated variable of the system (flow of base liter/min), $\text{PV}$ is the measured process variable (pH) and $\text{pH}_{\text{est}}$ is the estimated pH by the proposed ANFIS observer.

2. INVERSE pH MODELING
The titration curve can describe the nonlinearity of the pH process as shown in Fig.3. The curve starts with a linear behavior at the initial region; afterwards, the nonlinear behavior is initiated in the second region where a slight difference in volume or flow rate of the base will lead to a great variation of pH values. The sudden variation of the pH in the second region of the titration curve could endanger the stability of the control system, which is designed to maintain pH at a reference point. On the other hand, alternating from weak to strong acid or vice versa could cause instability of the process. This is due to the huge variations of the steady state gain endured in the switching process, (i.e. the gain of the strong acid at steady state is 350 times the weak acid gain) as noted in [2].

Obtaining the titration curve for a weak/strong acid - strong base is a challenging procedure, since the titration curve consists of several regions that behave in a different manner according to the $[\text{H}^+]$ in the solution. The titration operation is shown in Fig.2.

Eqs. (1) and (2) illustrates the volumetric concentration changes for acid and base streams.

$$V \frac{dc_{wa}}{dt} = Q_a C_a - (Q_a + Q_b) c_{wa}$$
(1)

$$V \frac{dc_{wb}}{dt} = Q_b C_b - (Q_a + Q_b) c_{wb}$$
(2)

$$-k c_{wa} + c_{wb} + 10^{-\text{pH}} - 10^{\text{pH}-14} = 0$$
(3)

Where; $c_{wa}$ and $c_{wb}$ are the concentration values of acid and base in the outlet stream, $Q_a$ and $Q_b$ are the volumetric flow rates of acid and base entering the reactor, $V$ is the reactor volume and $k$ is a constant indicates the strength of acid entering the reactor and given as:
\[ k = \frac{1}{1 + 10^{pK_a - pH}} \quad \text{For weak acid} \]  

Where \( K_a \) is the acid dissociation constant; \( pK_a = -\log_{10}(K_a) \), at steady state condition where both derivatives of \( c_{wa}, c_{wb} \) is substituted as Zero. By solving Eqs. (1) and (2) for \( c_{wa}, c_{wb} \) values and substitute it in Eq. (3) we will get:

\[ \frac{-kQ_aC_a}{Q_a + Q_b} + \frac{Q_aC_b}{Q_a + Q_b} + 10^{-pH} - 10^{pH - 14} = 0 \]  

(6)

From Eq. (6), \( Q_b \) could be obtained, simply as:

\[ Q_b = Q_a \frac{kC_a - 10^{-pH} + 10^{pH - 14}}{c_b + 10^{-pH} - 10^{pH - 14}} \]  

(7)

Solve for the titration curve in the form of \( pH = f(Q_b) \):

\[ pH = \log_{10} \left[ \frac{-\left( \frac{kQ_aC_a}{Q_a + Q_b} - \frac{Q_aC_b}{Q_a + Q_b} \right) + \left( \frac{kQ_aC_a}{Q_a + Q_b} - \frac{Q_aC_b}{Q_a + Q_b} \right)^2 - 4(10^{-14})(-1)}{2(10^{-14})} \right] \]  

(8)

Eq. (8) evaluates \( pH \) values according to the variation of the \( Q_b \) and consequently produces the titration curve for strong/weak acid – strong base. For the strong acid system the titration process is simpler because of large dissociation constant, which is responsible for the dissociation of the entire amount of acid into ions to be consumed by the disassociated base ions to form the simple molecules of salt and water.

Assuming that: \( C_a = 0.02 \) [mol.l\(^{-1}\)] for weak and strong acid, \( C_b = 0.025 \) [mol.l\(^{-1}\)], \( Q_a = 1.25 \) [l/min] and \( K_a = \infty \) for strong acid. The small dissociation constant of the weak acid prevents the base from consuming an equal amount from the weak acid due to incomplete disassociation of the weak acid into an acid ions (base conjugate), and hydrogen ions [6, 7]. The titration curve of the weak acid system is obtained by substituting \( (K_a) \) of the weak acid \( (K_a = 1.83x10^{-5}) \). Fig. 3 shows the obtained titration curves of Eq. (8) for weak/strong acid – strong base.

![Titration curves for strong/weak acid – strong base](image)

**Figure 3.** Titration curves for strong/weak acid – strong base.

Fig. 3 shows the difference in titration curve between weak acid system and a strong acid system. It worth to mention that the weak acid titration curve is smoother as shown in this figure, this is due to what is called as the "Buffering “ effect [8].

3. **DESIGN OF ADAPTIVE NEURO-FUZZY pH OBSERVER**

The ANFIS observer is an empirical model designed to replace the pH meter. The designed ANFIS model attempts to match nonlinearity and parametric uncertainties encountered with such dynamic process [9], and it has been proposed also to overcome the typical difficulties faced with using pH meters in chemical plants as wiring issues, troubleshooting, and maintenance of the system [6]. The proposed observer requires an evaluation of all variables that might affect the pH. The fuzzy inference process is implemented as a generalized neural network, which is then adjusted by a combination of least squares estimation and backpropagation algorithm [10]. The fuzzy rules and the
range of the membership functions are optimized to minimize the output error between the output of the fuzzy model and the input data. Fig. 4 shows the architecture of the implemented five-layer ANFIS system of Sugeno type [11].

The first layer is the input layer, the 2-input vectors are shown in Fig. 4: $x_1$: flow rate of base and $x_2$: temperate variation. The corresponding output of input $x_i$ at node $(i)$ in layer (1) is $O_{t,i}^1$. Layer 1 contains $k$ nodes for every input, which correspond to bell membership functions (BMF), $\mu$, according to:

$$O_{t,i}^1 = \mu_{A_{i,j}}(x_j), \ i=1,2,...k, \ j=1,2.$$  \hspace{1cm} (9)

Here, $A_{i,j}$ are fuzzy sets describing the input, while $\mu_{A_{i,j}}(x_j)$ is the degree of membership of a variable $x_j$ into the fuzzy set $A_{i,j}$. To calculate the firing strength of the $m^{th}$ rule (total $n$ rules) in layer 2, $w_m$, the rule output is equal to the product of incoming inputs from layer 1:

$$O_m^2 = w_m = \prod_{m=1}^{n} \mu_{A_{i,j}}(x_j), \ i, j \text{ are defined in } m^{th} \text{ rule.}$$  \hspace{1cm} (10)

The process continues to layer 3, the $m^{th}$ node computes the ratio of the $m^{th}$ rule’s firing strength to the sum of firing strength (normalization):

$$O_m^3 = \frac{w_m}{\sum_{m=1}^{n} w_m}.$$  \hspace{1cm} (11)

Layer 4: Each node in this layer represents a rule; it has adaptive nodes with corresponding functions:

$$O_m^4 = \bar{w}_m \times f_m$$  \hspace{1cm} (12)

where $f_m$ is a crisp variable of $m^{th}$ rule to describe the output. The last layer 5 has a single node, which computes the output (indentation loads) as the summation of layer 4 outputs:

$$O_5^f = \sum_{m=1}^{n} \bar{w}_m \times f_m$$  \hspace{1cm} (13)

The implemented learning algorithms involve unsupervised learning of the BMF (i.e. centers and widths) followed by unsupervised learning of the rules (calculation of rules and updates), and error back propagation for optimization of the membership functions (The output and the error are fed back to layer 2). Different data sets were used to validate the accuracy of the model.

The designed observer is validated experimentally to determine pH values (as a process variable in the control scheme) through measuring of $Q_b$ (as a manipulated variable in control scheme). To examine the designed observer, the estimated pH values were compared with experimental results to find the absolute average testing error, which was about 0.019, as shown in Fig.5.
Finally, the designed and validated observer is employed in the feedback design of the control loop as seen in Fig.1.

4. MULTIREGIONAL FUZZY-BASED CASCADE CONTROL STRUCTURE

The cascade control structure is very common in chemical processes. The proposed multiregional fuzzy-based cascade control structure, shown in Fig.1, consists of two main loops: the master loop (outer loop) where multiregional fuzzy PI controller is used, and the slave loop (inner loop) where a Weiner model-based fuzzy P controller is implemented, these interacting loops work together to obtain the optimal control over the process [12]. In the case of strong acid system, the nonlinear gain of the process output will be canceled out with the inversed function of the process (shown in Fig.1 which uses a constant $K_a$ of infinity for a strong acid), and accordingly the process control is achieved within the inner loop. Although in a case of a weak acid system, the process output gain will not be canceled out completely with the inverse function, and therefore the residue will be corrected within the outer loop. The proposed fuzzy controller will overcome the nonlinearity of the titration curve by partitioning the titration curve into three main regions [13, 14]. The Multiregional Fuzzy Controller will behave according to the determined region.

The controller has three inputs and only one output making the system as a multi-inputs single-output system (MISO). The inputs are: the error signal $e$, the error difference $\Delta e$ and an auxiliary variable (AV) which is control input that expresses the three regions of the titration curve, while the output is the actuating signal expressing ($\Delta Q_b$). The membership functions of each input and output is shown in Fig.6.

The inputs of $e$ and $\Delta e$ consists of five triangular membership functions ranging between (-1 and 1), while the third control input AV is expressed with three trapezoidal membership functions [15]. It’s representing the three regions of the titration curve ranging between (0 and 13). The output is more complicated than the inputs structure, it is represented using twelve triangular membership functions, with seven main functions that is used to perform the
aggressive variations needed during control, while the other five functions used for the fine control actions, the output's membership functions are ranging between (-1 and 1).

The Rules set of this controller are shown in table 1.

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<tr>
<th>Δe/e</th>
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Table 1. Rules set of multiregional fuzzy controller if ((a): AV is high or low for linear regions with titration curve and (b): AV is Medium for highly nonlinear region). Where; P is positive, L is large, M is medium, S is small, ZO is zero and N is negative.

The response of the multiregional controller within the three regions of the titration curve, and towards the set point tracking is presented Fig. 7 and Fig. 8.

![Figure 7](image1.png)  
**Figure 7.** Performance of Closed Loop Structure with Multiregional Fuzzy Controller in Set point Tracking (a) for weak acid (b) for strong acid.  

![Figure 8](image2.png)  
**Figure 8.** Performance of control structure with multiregional Fuzzy controller in the three Regions of Titration Curve (a) for weak acid (b) for strong acid.

The above figures (7 and 8), clearly, show a superior performance of the multiregional fuzzy-based cascade controller over the titration process with minimal resulted errors. The proposed cascade control structure uses two fuzzy-based controllers (in master and slave loops shown in Fig.1), each behaves differently to obtain the improved response shown in Fig.8.
5. CONCLUSION
The troubles might be found with pH electrodes, used for pH measurements, have been resolved by proposing an ANFIS-based pH observer to optimize the size of overall plant with cost reduction to meet the industrial enquiries. The effectiveness of the proposed observer has been ensured. The nonlinear behavior exhibited by the pH process was tested using nonlinear intelligent-based cascade control. It proved to be the best technique that could be used with such systems comparing with other nonlinear classical cascade ones that suffering from problems of parameter tuning.

6. REFERENCES